Consider the polar equation 
$$r = \frac{48}{5 - 7\sin\theta}$$
.

$$r = \frac{48}{1 - \frac{1}{5} \sin \theta} = \frac{48}{2}$$

$$e = \frac{1}{5} = \frac{48}{5} = \frac{48}{5}$$

$$p = \frac{48}{7}$$

$$y = -\frac{48}{7}$$

[b] Find the <u>rectangular</u> coordinates of the endpoints of <u>all</u> latera recta. <u>Do NOT convert the equation to rectangular.</u>

$$\frac{O}{O} = \frac{(x,y)}{(485,0)}$$

$$\frac{7}{1} - 24 = (0,-24)$$

$$\frac{7}{1} + 485 = (-485,0)$$

$$\frac{377}{2} + (0,-4)$$

CENTER = 
$$(0, \frac{24+4}{2}) = (0, -14)(2)$$
  
FOCI =  $(0, 2*-14)$  AND  $(0, 0)$   
=  $(0, -28), (0, 0)$ 

ENDS OF = 
$$(\pm 4\%5, -28)$$
,  $(\pm 4\%5, 0)$   
LR.  $(\pm 4\%5, -28)$ ,  $(\pm 4\%5, 0)$ 

[a] Find the co-ordinates of the focus/foci.

[b]

$$2(x^2+2x)-(y^2-1by)=16$$

$$\frac{(y-8)^{2}-(x+1)^{2}-1}{36-36-36-36-36}$$

$$c^{2}=36+3=39 \implies c=\sqrt{39}$$

If the equation corresponds to a parabola, find its directrix. If the equation corresponds to an ellipse, find the endpoints of its minor axis.

If the equation corresponds to a hyperbola, find the equations of its asymptotes.

SCORE: / 25 PTS

## The following symmetry tests do NOT indicate that the graph is symmetric: $(-r, -\theta), (-r, \pi-\theta)$ and $(r, \pi-\theta)$

[a] Using the results above, along with the tests and shortcuts shown in lecture, determine if the graph is symmetric over the polar axis,  $\theta = \frac{\pi}{2}$  and/or the pole. Summarize your conclusions in the table on the right.

NOTE: Run as FEW tests as needed to prove your conclusions are correct.

DDI AD AVIS	1 (r,-0) r= 2-sm2(0)		
POLARXIO	2 r= 2+5m2+	Type of symmetry	Conclusion
	(2) = 2+Sm 20	Over the polar axis	NO CONCLUSIO
POLE:	(r.0)-r= 2-sin20,	Over $\theta = \frac{\pi}{2}$	NO CONCLUSION
	0 r= -2+5m20	Over the pole	SYMMETRIC
*	$(r, \pi + \theta) r = 2 - \sin 2(\pi - \theta) r = 2 - \sin 2\pi - \sin 2\pi$	+20)	3

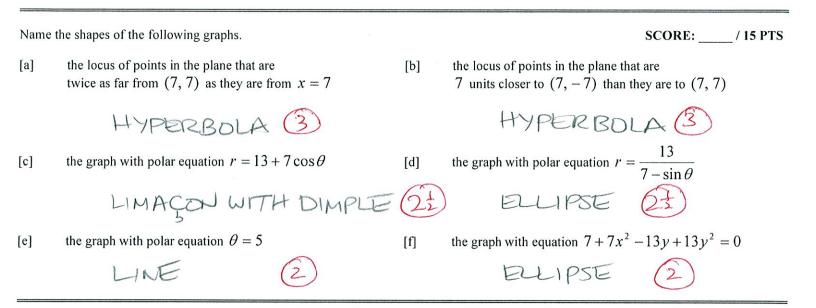
Based on the results of part [a], what is the minimum interval of the graph you need to plot (before using reflections to draw the rest of the graph)?

Find the <u>rectangular</u> equation of the parabola with focus (-5, 7) and directrix x = 13.

SCORE: \_\_\_\_/15 PTS

VEXTEX =  $\left(-\frac{5+13}{2}, \frac{7}{2}\right) = \left(4, \frac{7}{2}\right)$ 

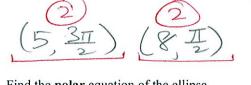
P= DIRECTED FROM VERTEX TO FOCUS = 
$$-15-4=-9$$
 $(y-7)^2 = 4(-9)(x-4)$ 
 $(y-7)^2 = -36(x-4)$ 

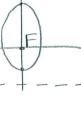


An ellipse has a focus at the pole and vertices with <u>rectangular</u> co-ordinates (0, -5) and (0, 8).

[a] Give polar co-ordinates for the vertices, using positive values of r and  $\theta$ .



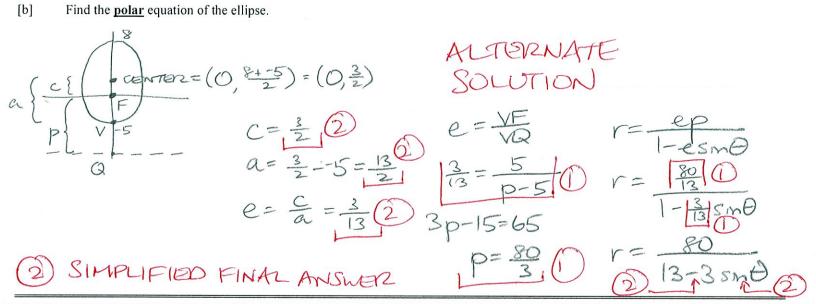




$$\frac{69.5+5e=8-8e}{13e=3}$$

$$e=\frac{3}{13}$$

$$=5+\frac{15}{13}$$
  
=  $65+15$ 

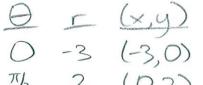


Consider	the	polar	equation	r	=	2	- 5	5 cos	$\theta$	
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SCORE: /30 PTS

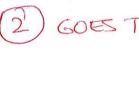
[a] Sketch the graph of the polar equation using the shortcut process shown in lecture / PowerPoint.

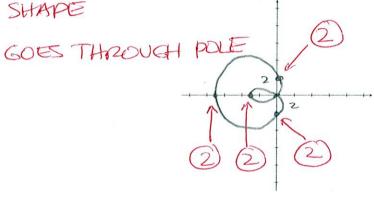
Label the scale on your axes clearly.



$$\frac{\pi}{3\pi}$$
 7 (-7,0)  $\frac{\pi}{2}$  (0,-2)

SHAPE





[b] Convert the equation to rectangular.

$$x^2 = 2r - 5r \cos \theta$$
 (3)  
 $x^2 + y^2 = 2\sqrt{x^2 + y^2} - 5x$ 

$$\frac{x^{2}+y^{2}+5x}{(x^{2}+y^{2}+5x)^{2}} = 4x^{2}+4x$$

$$r = 2 - \frac{5x}{3}$$
 $r^2 = 2r - 5x (3)$ 

$$(x^2+y^2+5x)^2 = 4x^2+4y^2$$